

Arithmetic vs. Geometric

	Arithmetic	Geometric
Function	Linear	Exponential
Need to know	d = common difference Adding/Subtracting	r = common ratio Multiplying/Dividing
Recursive	$a_1 = \text{first term}$ $a_n = a_{n-1} + d$	$a_1 = \text{first term}$ $a_n = a_{n-1} \cdot r$
Explicit	$a_n = a_1 + (n-1)d$	$a_n = a_1(r)^{n-1}$

Is this Arithmetic or Geometric?

$$-8, -6, -4, \dots$$

Arithmetic: $-6 - (-8) = 2$; $-4 - (-6) = 2$

Geometric: $-6/-8 = .75$ ($3/4$); $-4/-6 = .66$ ($2/3$)

Write the Explicit rule? $a_n = a_1 + (n - 1)d$

Step 1: Find first term and common difference.

$$a_1 = -8$$

$$d = 2$$

Step 2: Substitute first term and common difference in to the explicit formula.

$$a_n = -8 + (n - 1)2$$

Step 3: Simplify the equation:

$$a_n = -8 + (n - 1)2$$

$$a_n = -8 + 2n - 2$$

$$a_n = -10 + 2n \text{ or } a_n = 2n - 10$$

Is this Arithmetic or Geometric?

4, 8, 16, ...



Arithmetic: $8 - 4 = 4$, $16 - 8 = 8$

Geometric: $8/4 = 2$, $16/8 = 2$

What is the 15th term? (use explicit form): $a_n = a_1(r)^{n-1}$

Step 1: Find the first term and common ratio.

$$a_1 = 4$$

common ratio: 2

Step 2: substitute the first term and common ratio into the formula.

$$a_n = 4(2)^{n-1}$$

Step 3: substitute the term you are looking for in for n.

$$a_{15} = 4(2)^{15-1}$$

Answer: $a_{15} = 65,536$